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## Complexity Theory

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*Due date: May 26, 2014 before class!*

### Problem 1 (10 Points)

Show that  $\text{SPACE}(n) \neq \mathcal{NP}$ . (Note that it is unknown if either class is contained in the other.)

### Problem 2 (10 Points)

Define the class  $\mathbf{E} = \bigcup_c \text{DTIME}(2^{cn})$ .

1. Is  $\mathbf{E}$  closed under polynomial-time reductions?
2. Show that  $\mathcal{P}^{\mathbf{E}} = \mathbf{EXP}$ .

### Problem 3 (10 Points)

1. Argue that at least one of the assumptions  $\mathbf{L} \neq \mathcal{P}$  and  $\mathcal{P} \neq \mathbf{PSPACE}$  is true.
2. Use padding to show that if  $\mathcal{P} = \mathbf{L}$ , then  $\mathbf{EXP} = \mathbf{PSPACE}$ .

### Problem 4 (10 Points)

Consider the problem of checking a boolean formula's syntactical correctness. Show that this problem can be decided in log-space, even if we have no precedence relation between the boolean operators and force precedence behavior with parentheses, e.g.  $(x \wedge y) \vee (\bar{z} \wedge x) \vee \bar{y} \vee z$  is a valid formula, as is  $(x \wedge (y \vee \bar{z}) \wedge x) \vee \bar{y} \vee z$ , while  $x \wedge y \vee \bar{z} \wedge x \vee \bar{y} \vee z$  is not.